

Killing Stubborn Mutants with Symbolic Execution

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Mutation

program

```

Maximum (a, b, c)
1. max = a;
2. if (b > max)
3.   max = b;
4. if (c > max)
5.   max = c;
6. return max;
    
```

Mutation operators

- > → !=
- = → +=
- > → <

Mutant

```

Maximum (a, b, c)
1. max = a;
2. if (b != max)
3.   max = b;
4. if (c > max)
5.   max = c;
6. return max;
    
```

Mutant

```

Maximum (a, b, c)
1. max = a;
2. if (b > max)
3.   max = b;
4. if (c != max)
5.   max = c;
6. return max;
    
```

Mutant

```

Maximum (a, b, c)
1. max = a;
2. if (b > max)
3.   max = b;
4. if (c > max)
5.   max = c;
6. return max;
    
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Mutant

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Mutant

```

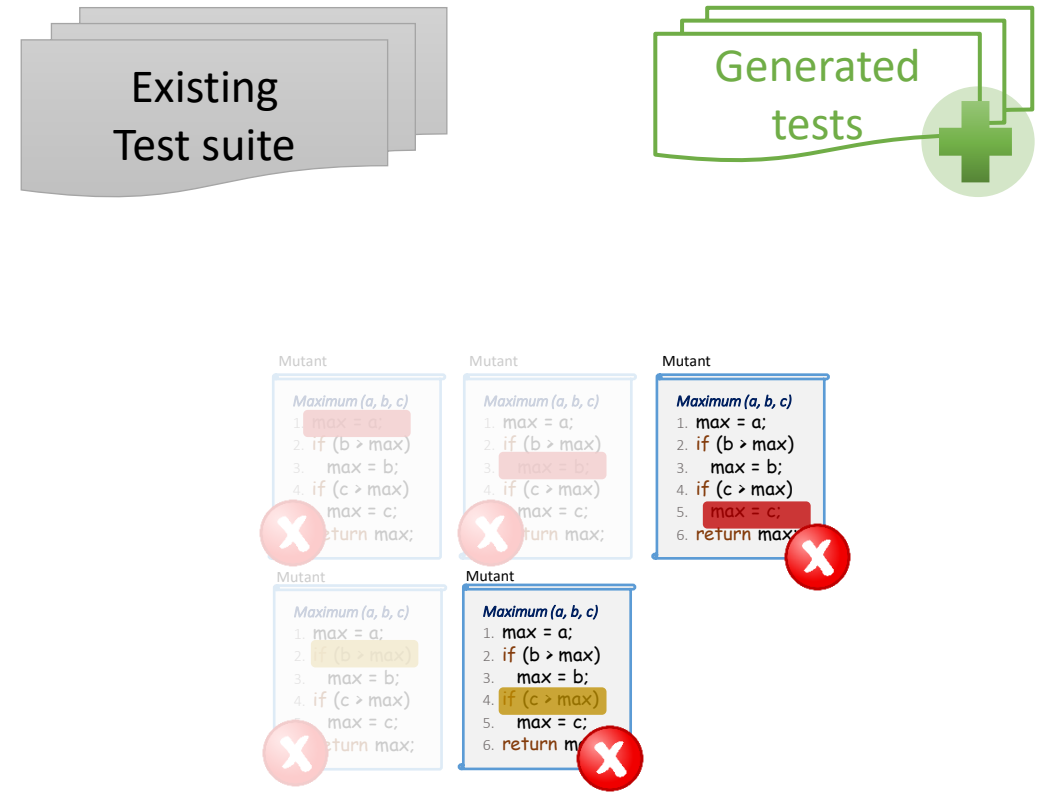
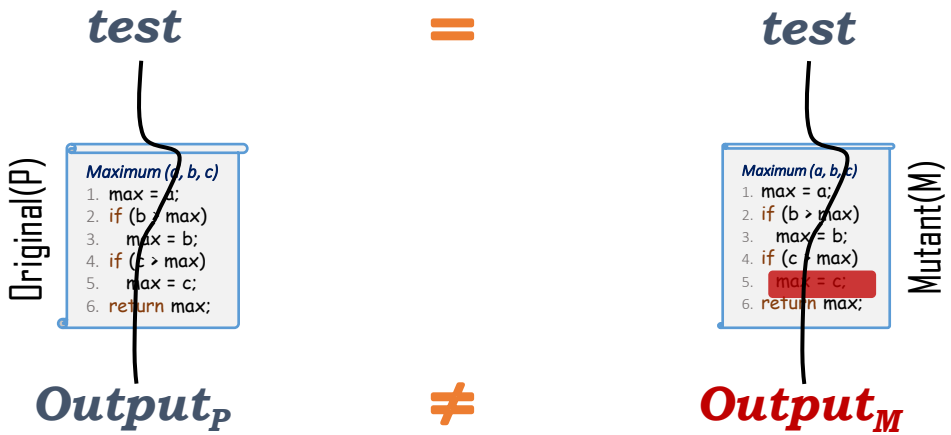
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Mutant

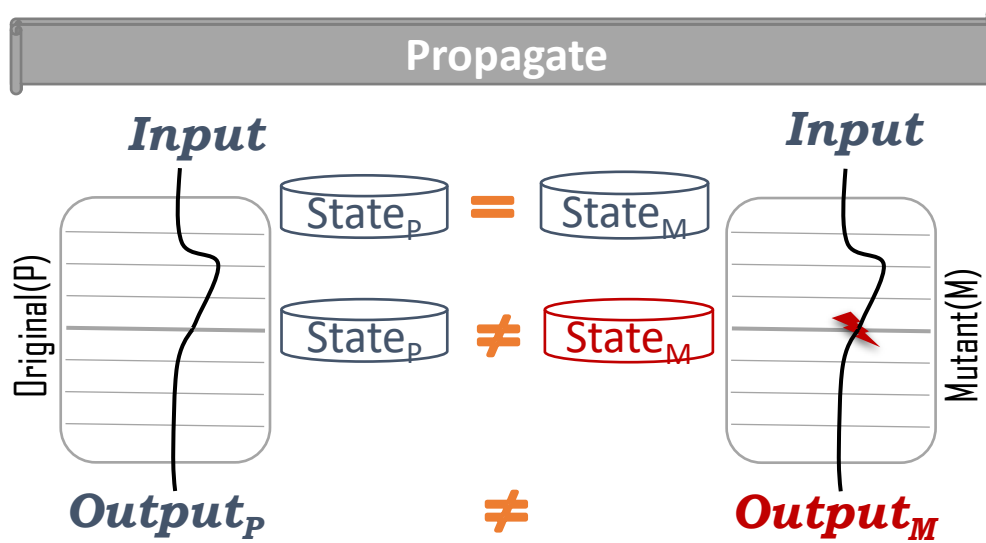
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Maximum (a, b, c)
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Mutation

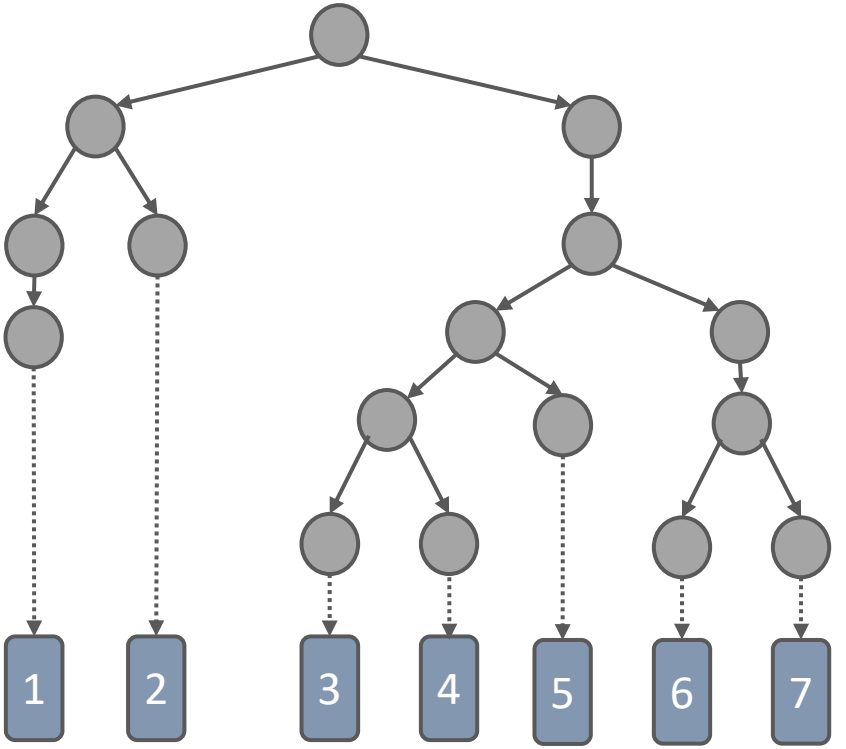


Mutant Killing

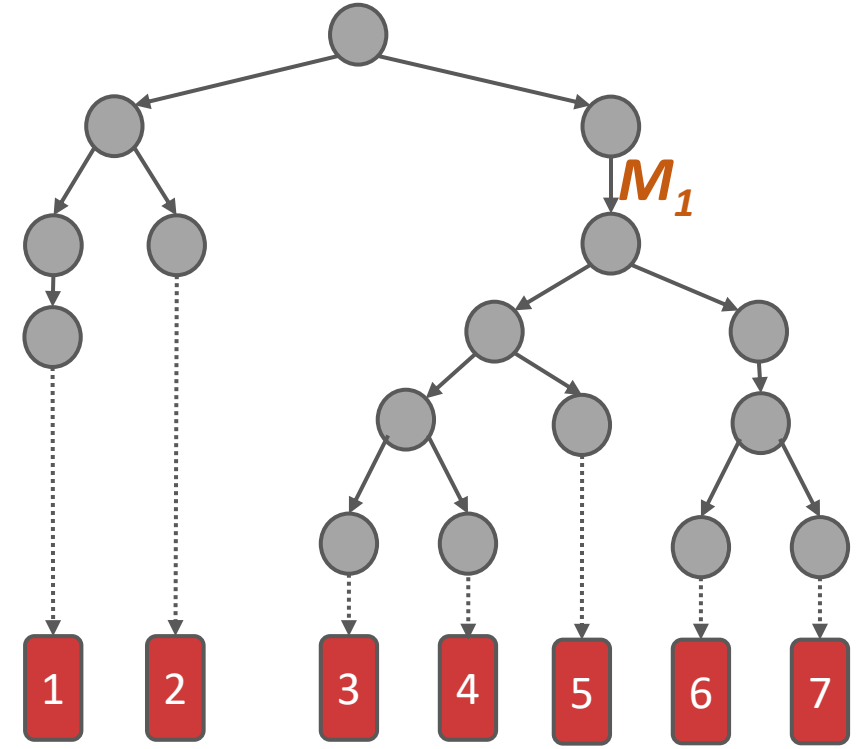


Symbolic Mutant Test Generation

Original

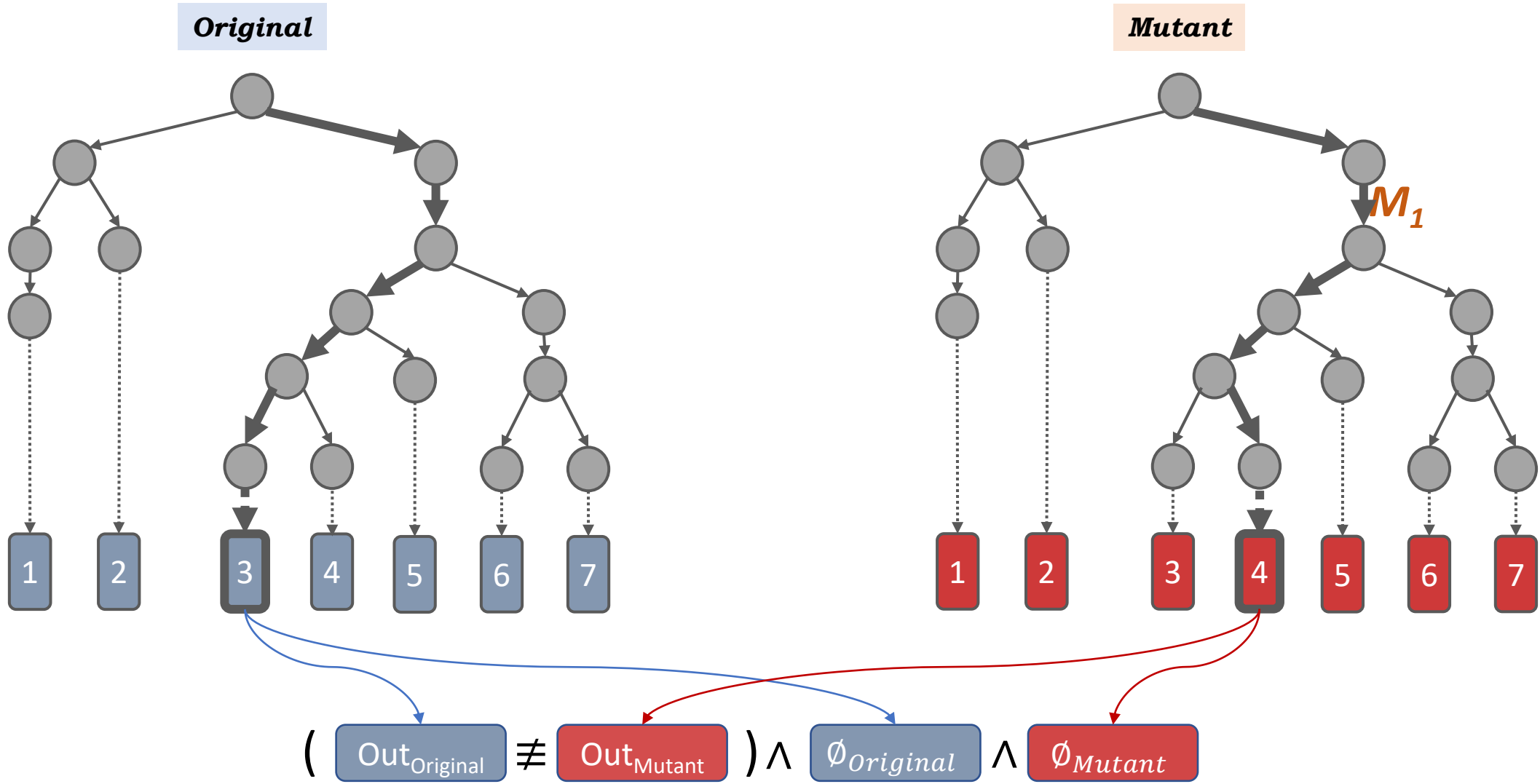


Mutant



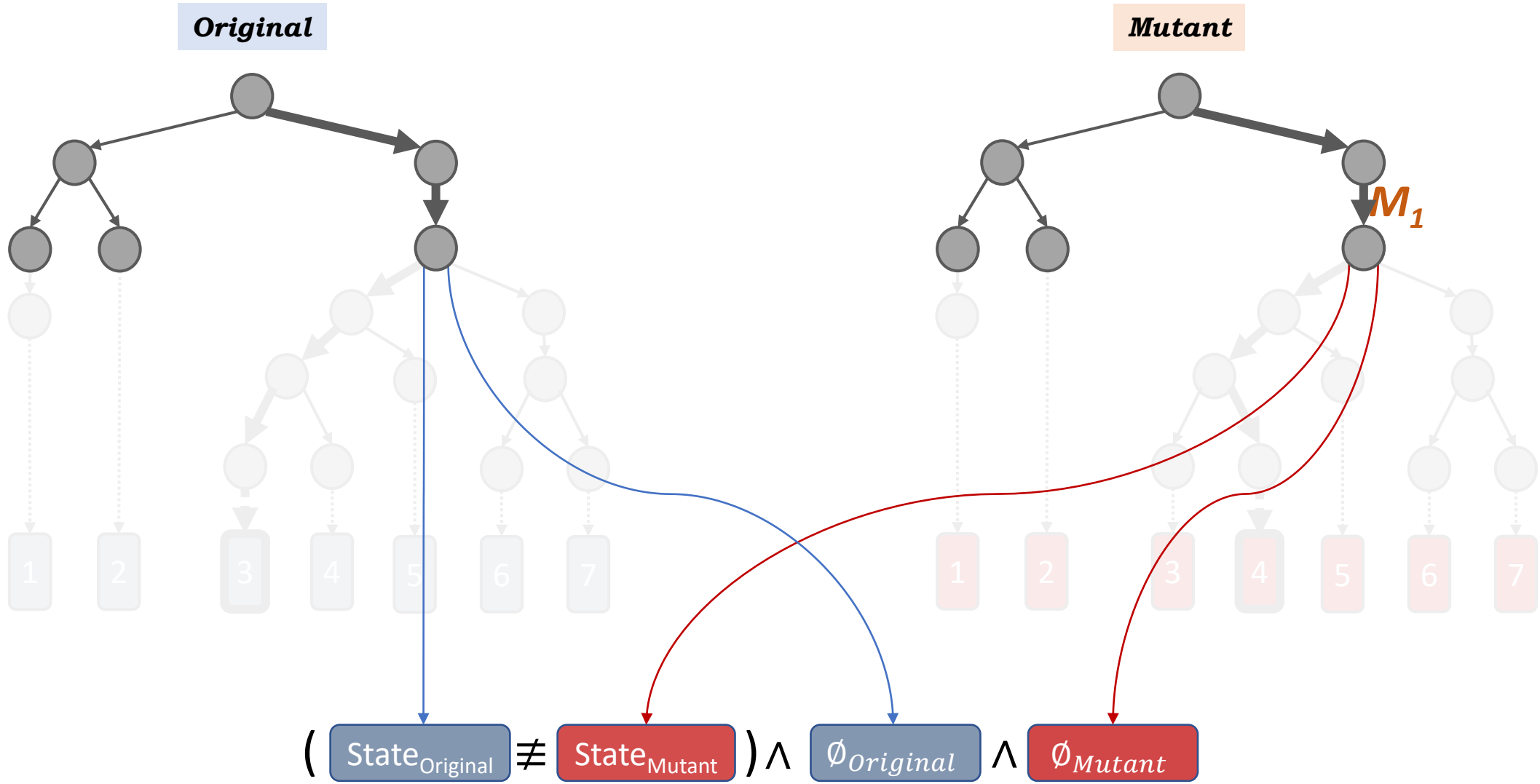
← Path ID →

Symbolic Mutant Test Generation



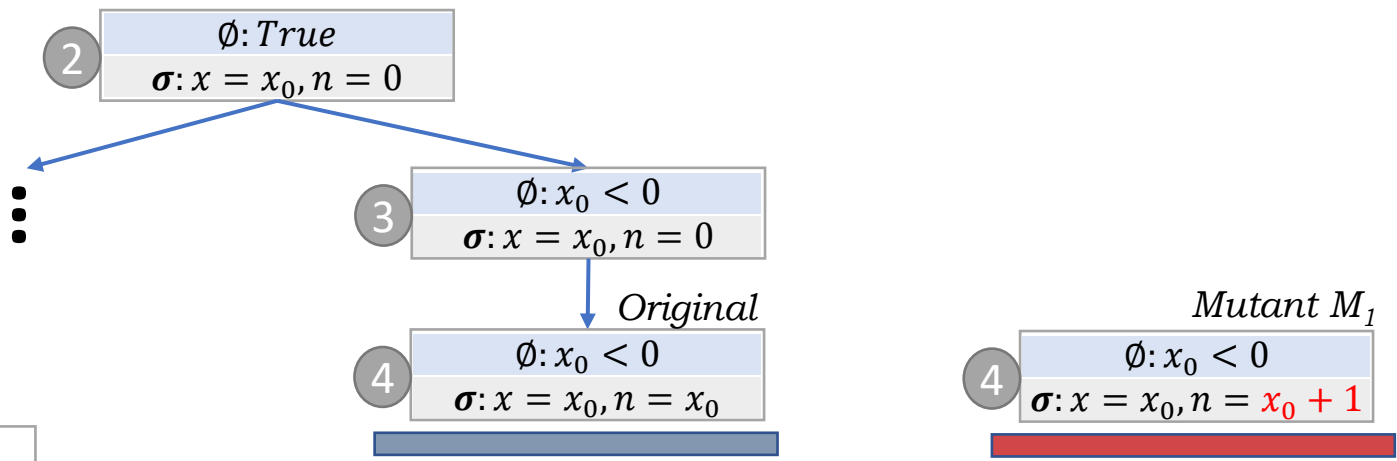
Symbolic Mutant Test Generation

Infect-only



Symbolic Mutant Test Generation

Infect-only



Program

```

int func (int x) {
1. int n = 0;
2. if (x < 0) {
3.     n = x; // M1 (n = x + 1);
4.     if (n)
5.         n++;
}
7. return n;
}
  
```

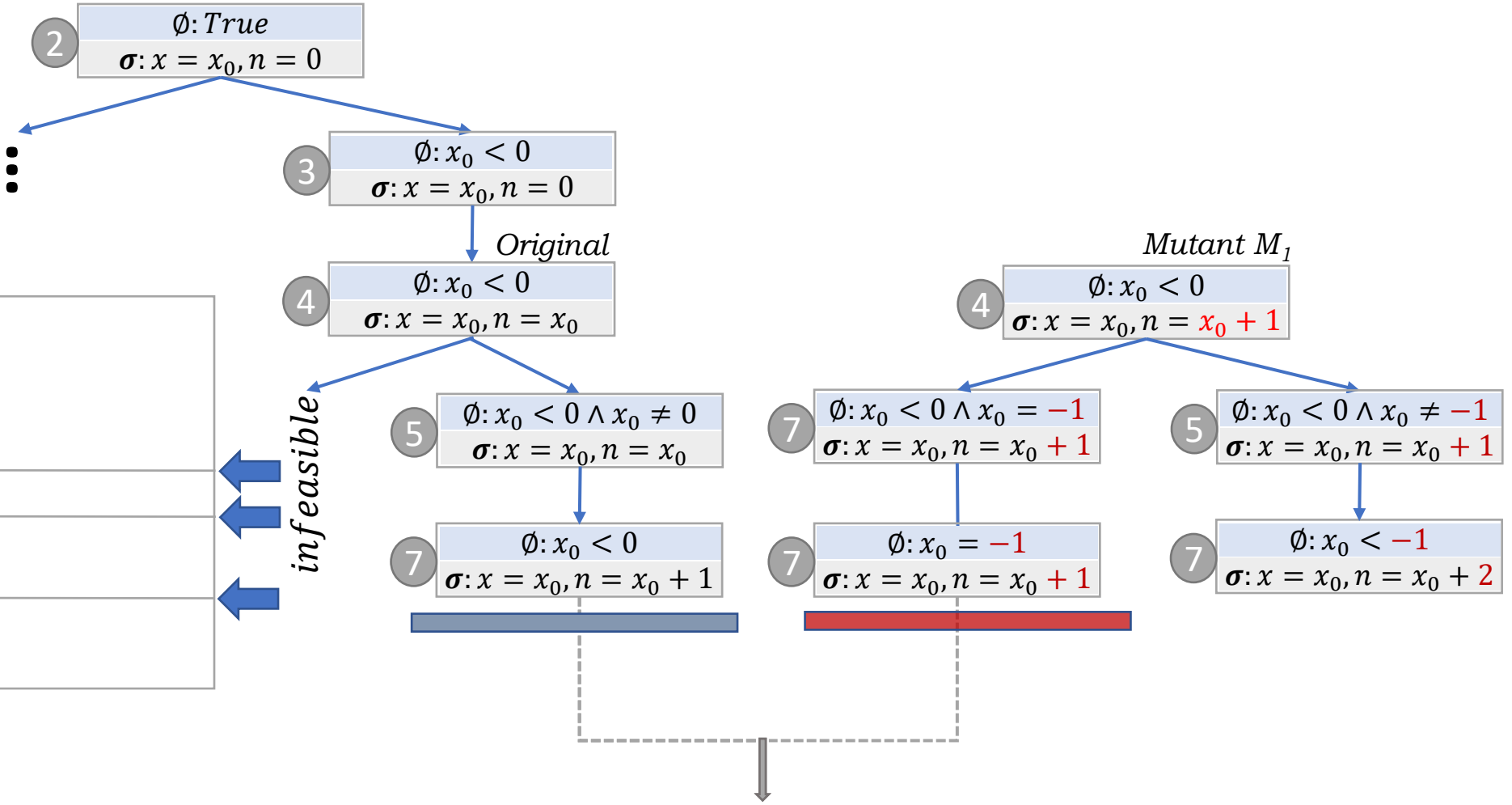
The mutant M₁ is not killed by the test

$$(\text{State}_{\text{Original}} \neq \text{State}_{\text{Mutant}}) \wedge \phi_{\text{Original}} \wedge \phi_{\text{Mutant}}$$

$$\left. \begin{array}{l} \text{Out}_{\text{Original}} = 0 \\ \text{Out}_{\text{Mutant}} = 0 \end{array} \right\} x_0 = -1 \xleftarrow{\text{Z3 solver}}$$

$$(\text{State}_{\text{Original}} \neq \text{State}_{\text{Mutant}}) \wedge \phi_{\text{Original}} \wedge \phi_{\text{Mutant}}$$

Symbolic Mutant Test Generation


Program

```

int func (int x) {
1.  int n = 0;
2.  if (x < 0) {
3.      n = x; // M1 (n = x + 1;)
4.      if (n)
5.          n++;
6.  }
7.  return n;
}
    
```

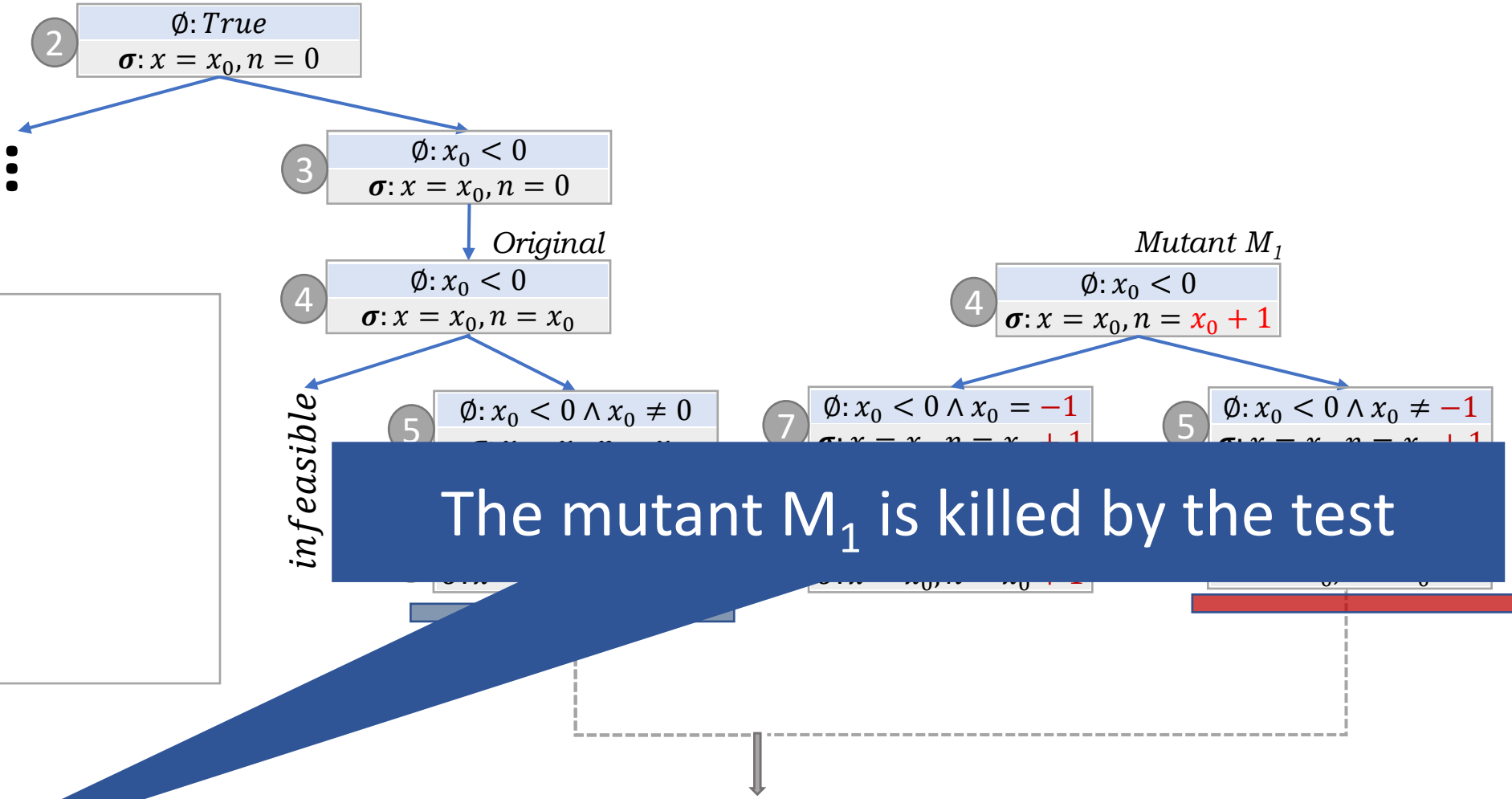
Infeasible ← Z3 solver ($x_0 + 1 \neq x_0 + 1$) \wedge $x_0 < 0$ \wedge $x_0 = -1$

Symbolic Mutant Test Generation

Program

```

int func (int x) {
1.  int n = 0;
2.  if (x < 0) {
3.      n = x; // M1 (n = x + 1);
4.      if (n)
5.          n++;
6.  }
7.  return n;
}
    
```



infeasible

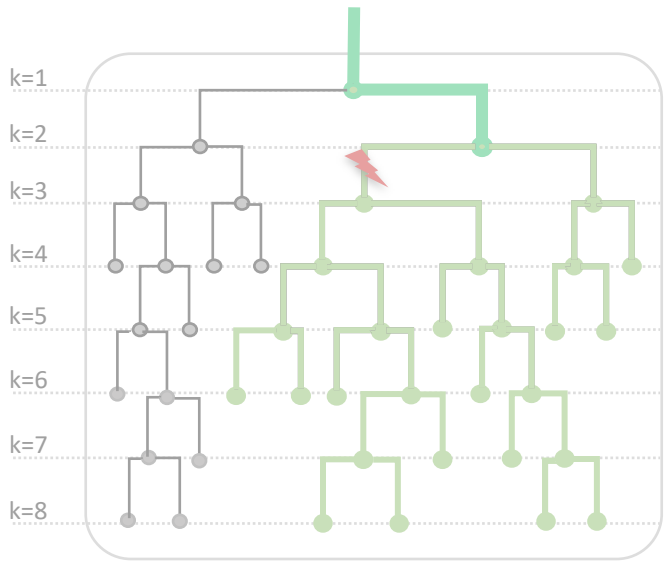
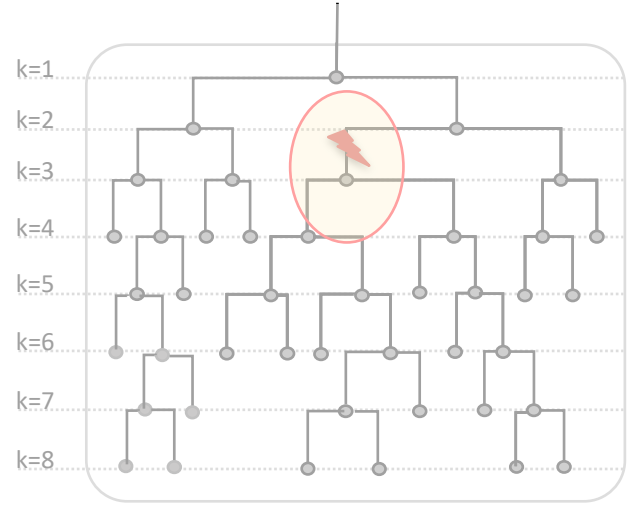
The mutant M₁ is killed by the test

$$\left. \begin{array}{l} Out_{Original} = -1 \\ Out_{Mutant} = 0 \end{array} \right\} x_0 = -2 \xleftarrow{\text{Z3 solver}} ((x_0 + 1 \neq x_0 + 2) \wedge x_0 < 0 \wedge x_0 < -1)$$

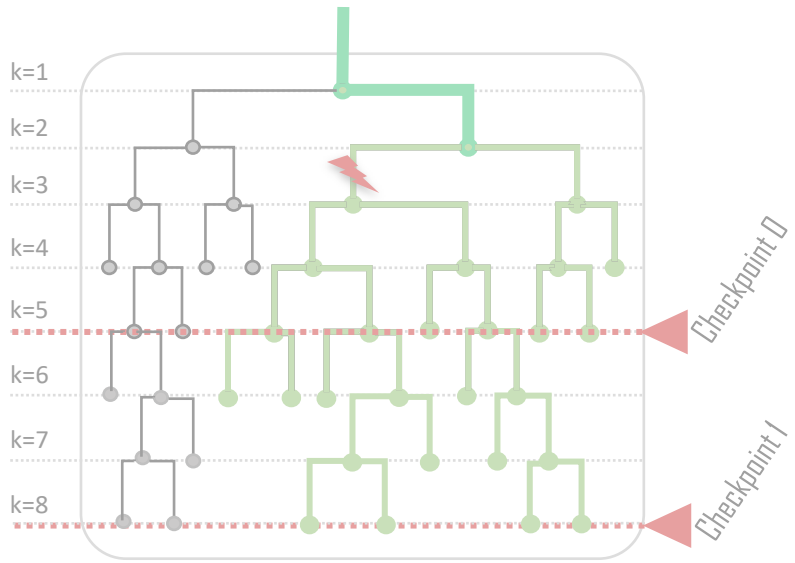
SEMu

SEMu implements heuristics that enable scalable and deeper mutant-error propagation

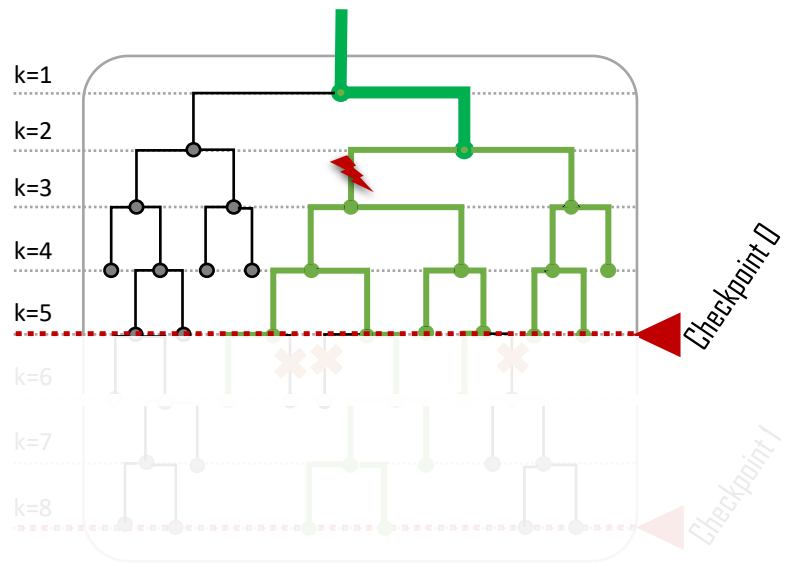
SEMu Cost-control Heuristics



(a)



(b)



(c)

Completeness Preserving Optimizations

Program

```

int func (int x) {
1.  int n = 0;
2.  if (x < 0) {
3.      n = x; // M1 (n = x + 1;) M2 (n += x;)
4.      if (n)
5.          n++;
        }
7.  return n;
}
    
```

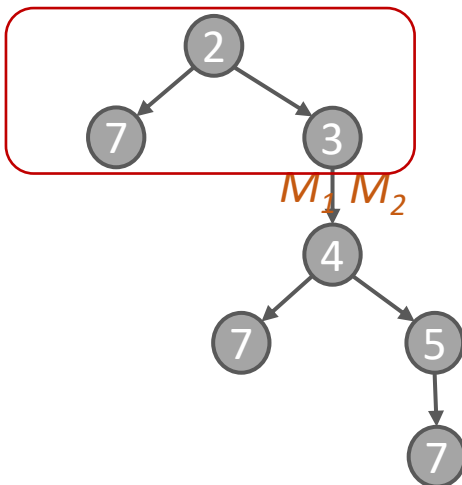


Meta-mutant Program

```

unsigned MUTANT_ID;
int func (int x) {
1.  int n = 0;
2.  if (x < 0) {
3.      switch(MUTANT_ID){
          case 1: n = x + 1; break;
          case 2: n += x; break;
          default: n = x;
        }
4.  if (n)
5.      n++;
        }
7.  return n;
}
    
```

Shared



Implementation

***SEMu* is implemented on KLEE**

Our implementation added/modified more than 8,000 lines of code.

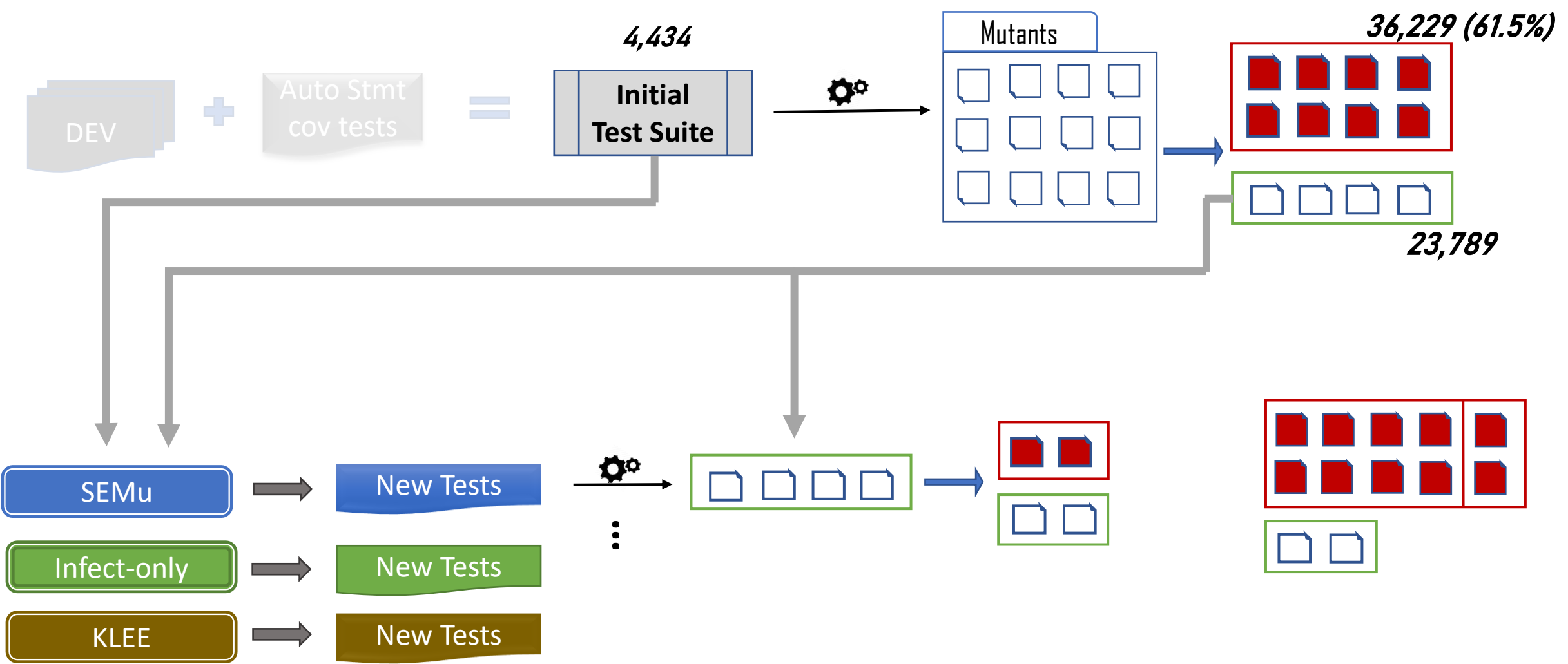
<https://github.com/thierry-tct/KLEE-SEMu>

Evaluation

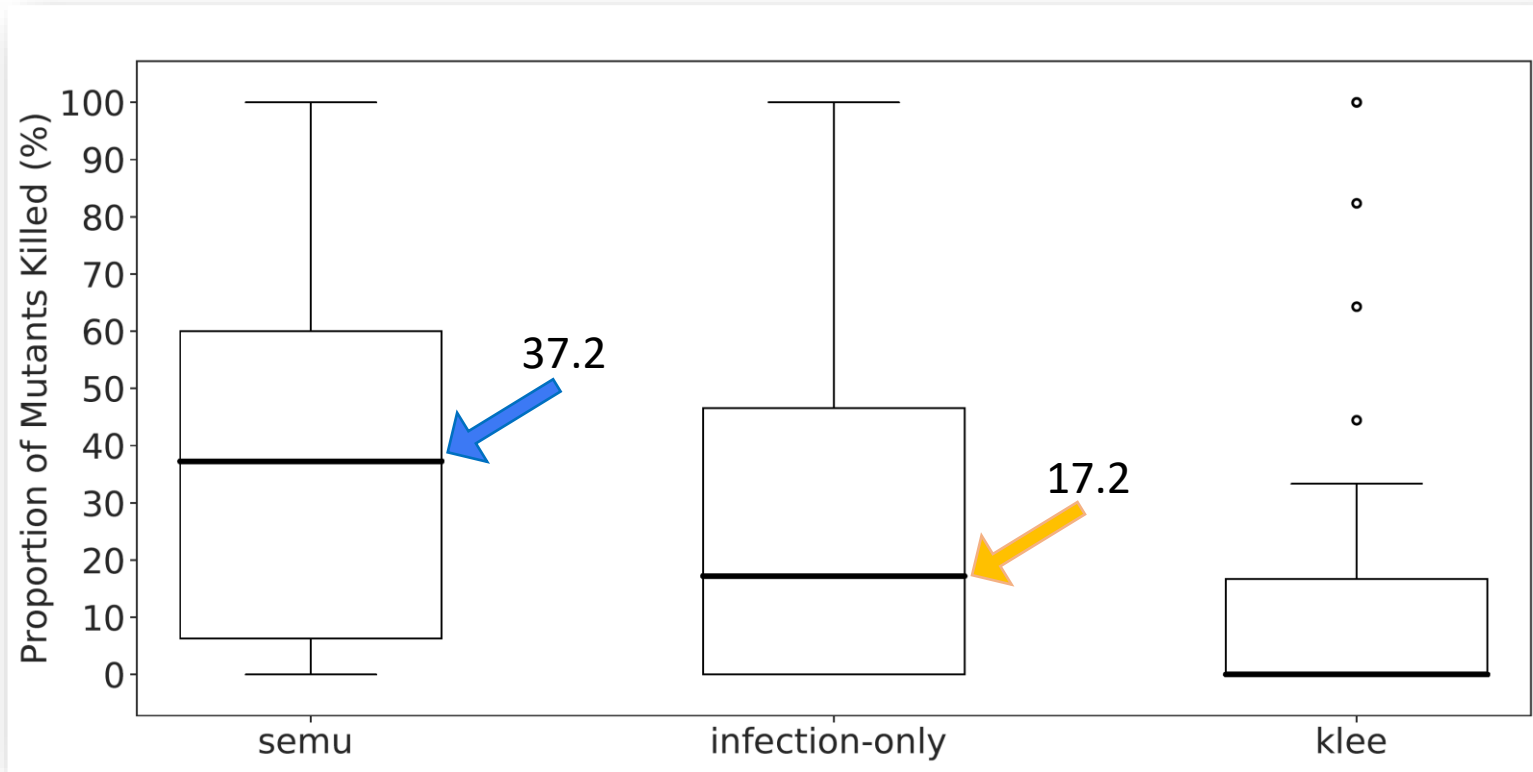
We evaluate *SEMu* and compare with KLEE and the state-of-the-art-approach (*infect-only*)

Subjects: 36 Programs from GNU Coreutils

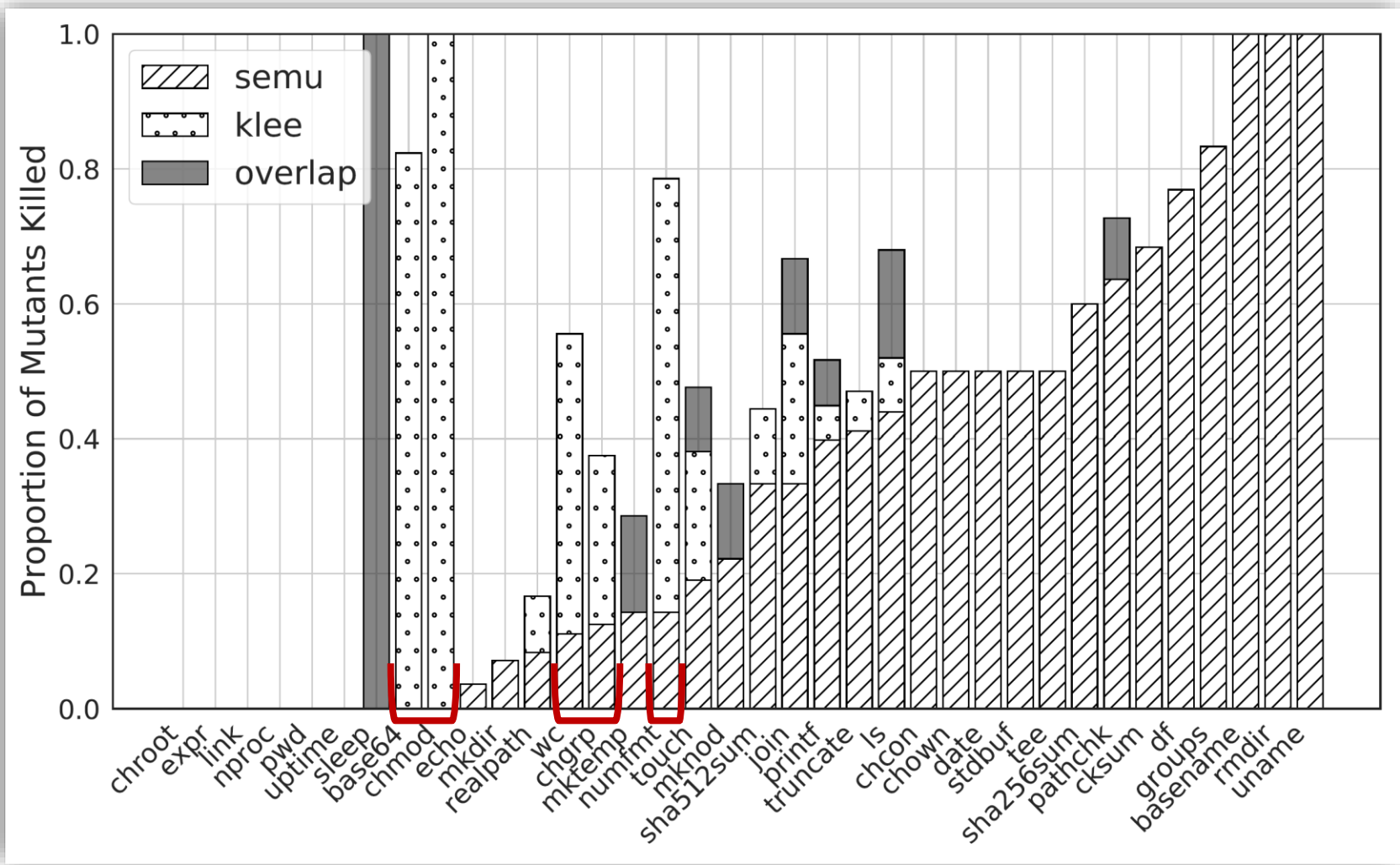
Evaluation - Procedure



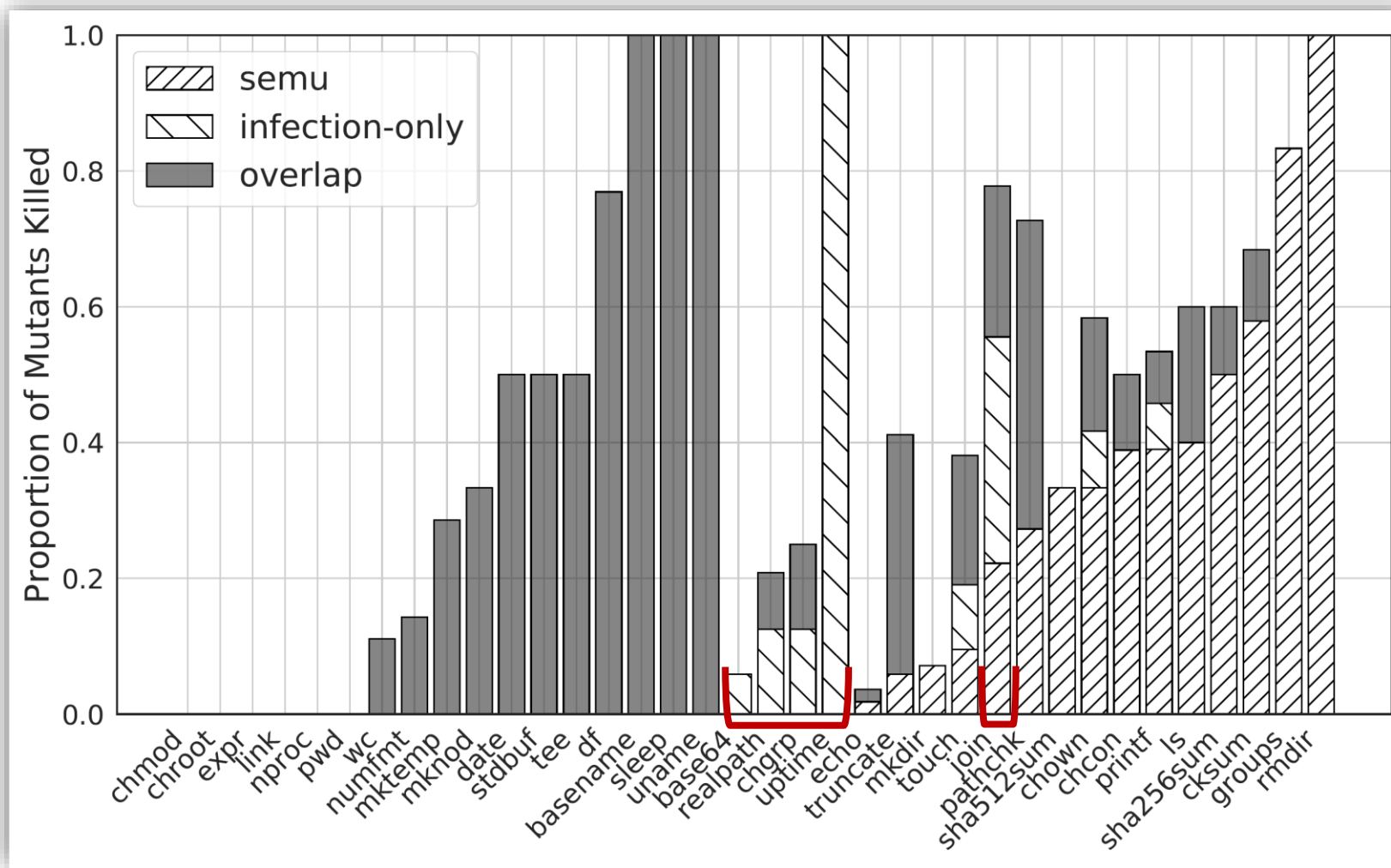
Evaluation - Results



Evaluation - Results



Evaluation - Results



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Mutation

test

Original(P)

Output_P

test

Mutant(M)

Output_M

≠

Existing Test suite

Generated tests

3

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Symbolic Mutant Test Generation

Infect-only

2

$\phi: \text{True}$
 $\sigma: x = x_0, n = 0$

3

$\phi: x_0 < 0$
 $\sigma: x = x_0, n = 0$

Original

4

$\phi: x_0 < 0$
 $\sigma: x = x_0, n = x_0$

4

Mutant M_1
 $\phi: x_0 < 0$
 $\sigma: x = x_0, n = x_0 + 1$

Program

```

int func (int x) {
1. int n = 0;
2. if (x < 0) {
3.   n = x; // M1 (n = x + 1;)
4.   if (n)
5.     n++;
6. }
7. return n;
}

```

The mutant M_1 is **not** killed by the test

$(\text{State}_{\text{Original}} \neq \text{State}_{\text{Mutant}}) \wedge \phi_{\text{Original}} \wedge \phi_{\text{Mutant}}$

$\text{Out}_{\text{Original}} = 0$
 $\text{Out}_{\text{Mutant}} = 0$ } $x_0 = -1$ $\xleftarrow{\exists$ solver

$(x_0 \neq x_0 + 1) \wedge x_0 < 0 \wedge x_0 < 0$

10

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SEMu Cost-control Heuristics

(a)

(b)

(c)

14

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Evaluation - Results

Method	Median (%)
semu	37.2
infection-only	17.2
klee	~10

21