4th International KLEE Workshop on Symbolic Execution

Symbolic Execution Oriented Constraint Solving

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Constraint solving is the enabling technique



Challenges of Symbolic Execution



Decision Procedures An Algorithmic Point of View, Second Edition, 2016



This Talk's Target

Decision Procedures An Algorithmic Point of View, Second Edition, 2016

Existing Work of Optimizing Constraint Solving in SE

- Query cache (partial) and simplification • KLEE[OSDI'08], KLEE-Array[ISSTA'17]
- Query reduction
 - SSE[ISSRE'12], Cloud9[PLDI'12]
- Query reuse
 - Green[FSE'12], GreenTrie[ISSTA'15]

Our Observation









Type and Interval Aware Array Constraint Solving [ISSTA 2021]



• Type and Interval Aware Array Constraint Solving [ISSTA 2021]



Partial Solution Prompted Symbolic Execution [ASE 20]



Type and Interval Aware Array Constraint Solving [ISSTA 2021]



Partial Solution **Prompted Symbolic** Execution [ASE 20]



Array Code Symbolic Execution

Arrays are ubiquitous in programs

The symbolic execution of array code is challenging



Array SMT Theory

Memory modeling in SE

Byte-level memory reasoning in symbolic execution
QF_ABV SMT theory

• KLEE、S2E、...

Memory modeling in SE

- Byte-level memory reasoning in symbolic execution
 - QF ABV SMT theory
 - KLEE, S2E, ...
- Every data is represented by a byte array
 - Many array variables in the path constraints
 - Large amount of axioms (O(n^2))

Problem

- - Byte-level array representation
 - Large number of axioms

Scalability of array constraint solving in symbolic execution

Our Key Insights

- Many redundant axioms exist for byte array constraints
 - Array access type information
 - Array index constraint

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- Many redundant axioms exist for byte array constraints Array access type information
- - Array index constraint
- Unsatisfiability can be decided earlier

Our Key Idea

- Utilize the information calculated during symbolic execution
 - Type information of array accesses
 - Interval information of array index variables

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- Utilize the information calculated during symbolic execution
 - Type information of array accesses
 - Interval information of array index variables
- Check the unsatisfiability earlier
- Remove redundant axioms during solving











$0 \le i \le 3 \land 0 \le j \le 3 \land i + j > 4$ \bigwedge R(a, i) + R(a, j) > 10

$$a[4] = \{0, 0, 0, 5\}$$

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$$a[4] = \{0, 0, 0, 9\}$$

Axiom elimination

Evaluation

- Research Questions
 - Effectiveness
 - Relevance of either optimization
 - Comparison with KLEE-Array

Evaluation

- Implementation
 - KLEE with STP
 - PPL solver for ILP solving

- Real-world programs as benchmark
 - Coreutils programs (62)
 - Lexer programs of various grammars (13)

Improves the queries for 46 programs, 160.52% on average

Results of Effectiveness

Improves the queries for 56 programs, 182.56% on average

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Results of Relevance

Opt 2 is more significant, while Opt 1 can generate useful information for Opt 2

Comparison with KLEE-Array

ne	KLEE-A	Irray	Our Method			
115	#Instrs	#Paths	#Instrs	#Paths		
	71687	29	63864	28		
	38892	24	53921	38		
х	599397	184	523956	165		
	69777	66	89288	86		
	353230	342	417394	401		
	87322	87	115455	124		
	35871	22	45190	35		
р	5221268	1554	14514660	4479		
	637629	3456	880674	5542		
	340874	36	440008	43		
rl	325398	338	379466	402		
e	665723	337	750713	421		
	373181619	489	373304921	584		

Our method increases the number of paths and instructions by 30.31% and 40.39%, respectively

 Type and Interval Aware Array **Constraint Solving** [ISSTA 2021]

Partial Solution Prompted Symbolic Execution [ASE 20]

Multiplex Symbolic Execution

• Double explosions in symbolic execution

path explosion in symbolic execution engine 51 combinatorial explosion in constraint solver

Multiplex Symbolic Execution

• Generate multiple test inputs by solving once

path explosioncombinatorial explosionin symbolic execution enginein constraint solver

▲ partial solution: C₁/\~C₂
 ↓
 ● partial solution: C₁/\C₂/\~C₃
 ■ solution: C₁/\C₂/\C₃

Partial Solution

1	<pre>public void start(int x, int y)</pre>
2	if (x + y >= 2) {
3	if(2 * y - x >= 1) {
4	if(2 * x - y >= 0) {
5	System.out.println(
6	<pre>} else {</pre>
7	System.out.println(
8	<pre>} Initial input: x =</pre>
9	} else {
10	System.out.println("#3
11	}
12	} else {
13	<pre>System.out.println("#4");</pre>
14	}
15	Path space and solut
	progra

53

tion space are related for the m's input space

Motivation Example First solving) { x = 0, y = 0Pivot ("#2"` ["#1"); x = 2, y = 0Pivot "); I, y = | $2y - x_{54} \ge 1 \wedge 2x - y \ge 0$

1	<pre>public void start(int x, int y)</pre>
2	if (x + y >= 2) {
3	if(2 * y - x >= 1) {
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5	System.out.println(
6	} else {
7	System.out.println(
8	}
9	} else {
10	System.out.println("#3
11	}
12	} else {
13	<pre>System.out.println("#4");</pre>
14	}
15	}
	$x + y \ge 2 \wedge 2y -$

Motivation Example First solving = 0, y = 0"#2") Pivot ntln("#1"); x = 2, y = 0 n("#3"); Pivot $x + y \ge 2 \wedge 2y - x \ge 1 \wedge 2x - y \ge 0$

1	<pre>public void start(int x, int y)</pre>
2	if (x + y >= 2) {
3	<pre>if(2 * y - x >= 1) {</pre>
4	if(2 * x - y >= 0) {
5	System.out.println('

Only need one time of solving

} else { 12 System.out.println("#4 13 14 15 }

Vanilla Symbolic Execution

Multiplex DSE (MuSE)

Utilize partial solutions for generating multiple tests by solving once during DSE

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Vanilla Symbolic Execution

Multiplex DSE (MuSE)

Partial Solutions are Ubiquitous

- CDCL/DPLL framework for SAT
- DPLL(T) framework for SMT

•

• JFS: coverage-guided fuzzing for FP constraints

Partial Solution Support

- What we have done
 - QF_LIA: Simplex-based
 - QF_ABV: CEGAR-based
 - Optimization-based floating-point solving

- Solvers with partial solution support
 - QF LIA on Z3
 - QF ABV on STP
 - Optimization-based floating-point solving (Simulated annealing-based Java implementation)
- C programs: Concolic KLEE + QF ABV(STP)
- Java programs: JFuzz + QF_LIA/QF_FP

Evaluation - Implementation

Simplex-baed QF_LIA solving

, > , >								
Drograms	DFS+P		DFS		BFS+P]	
Programs	#T	#NI	#T	#NI	#T	#NI	#	
BMPDecorder	1125	134	5	0	3746	84	10	
AviParser	340	117	144	46	1732	101	11	
GifParser	721	25	60	5	1905	64	96	
BMPParser	1203	52	8	0	4458	126	10	
PGMParser	264	1	263	1	4736	188	736	
ImgParserPCX	387	38	81	20	2596	76	6	
ImgParserBMP	458	314	114	21	1784	528	13	
JaadParser	2083	64	134	0	2692	64	283	
Schroeder	1149	23	235	20	2267	29	40	
JMP3Parser	214	286	37	198	319	653	27	
Toba	1836	344	117	87	1670	311	17	
Average	889	127	108	36	2536	202	113	

D(B)FS+P: D(B)FS + partial solution **#T**: the number of test inputs **#NI**: the number of new instructions covered after the first path

MuSE can cover more instructions

Evaluation - Result (1/3)

CEGAR-based QF_ABV

	DF	S+P	BF	S+P	Other Stategies			
Programs	#PS	COV	#PS	COV	RCN	RSS	DFS	BFS
akimaei	1	64.7	514	76.1	76.5	67.2	65.3	64.9
bilinea	305	71.6	172	80.8	79.0	77.4	59.1	65.4
find	177	96.9	156	96.7	91.3	40.0	91.5	97.7
eigengs	19	73.5	118	98.0	67.6	51.6	61.1	82.8
fft-rrt	1015	46.8	350	99.5	39.6	38.6	46.5	11.3
h2d-ps	4	95.7	130	98.6	47.5	47.5	95.7	98.6
sort	18	100.0	9	100.0	89.7	82.2	83.7	44.6
sum-lu	29	76.5	129	88.6	70.8	50.7	70.1	43.1
linear-ed	13	63.1	1015	82.8	79.9	78.7	56.3	63.8
linear-ei	3	73.5	376	80.5	77.5	71.2	64.2	72.6
solve-ct	135	93.4	33	94.4	26.6	22.3	13.8	93.5
solve-ctn	32	94.2	2	96.0	21.7	19.2	30.0	95.5
steffen-ei	18	74.8	253	83.4	68.7	65.6	67.4	68.8
Average	136	78.8	250	90.4	64.3	54.8	61.9	69.4

D(B)FS+P: D(B)FS + partial solution **#PS**: the number of partial solutions **COV**: LLVM code coverage

MuSE can achieve higher coverage

Evaluation - Result (2/3)

Optimization-based Floating-point Solving

Drograms	DFS+P		DFS		BFS+P		BFS	
Programs	#T	#NI	#T	#NI	#T	#NI	#T	#N
EigenD	3	244	1	0	477	1028	20	96
JacobiS	1424	13	43	6	1151	13	43	
CholeskyD	1376	1335	43	4	1116	8	42	
LeastS	169	2000	1	0	573	2246	43	219
SquareR	1541	166	43	4	1240	8	44	
EDAnalysis	8	418*	3	3*	8	392*	3	
Mutil	10	7*	4	0*	10	7*	4	(
RankAnalysis	255	406	15	180	325	427*	20	427
SVDAnalysis	204	427*	38	418*	276	427*	19	422
TVSAnalysis	343	430	1	0	484	612	7	22
Average	484	495	17	55	514	469	22	38

D(B)FS+P: D(B)FS + partial solution **#T**: the number of test inputs **#NI**: the number of new instructions covered after the first path

MuSE can cover more instructions

Evaluation - Result (3/3)

Follow-up Work

Utilize partial solutions to enrich solving cache and improve cache hit

Discussion

- Challenges
 - How to unify the explorations of the path space and the solution space?
 - How to sample the solving procedure?

Summary

 Type and Interval Aware Array Constraint Solving [ISSTA'21]

 Partial Solution Promoted Symbolic Execution [ASE'20]

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Thank you! \mathbf{O}

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